## Moving object detection, tracking and following using an omnidirectional camera on a mobile robot

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## Outline

(1) Introduction
(2) Detecting motion

Image formation
Detection of moving objects on the sphere
(3) Tracking on the unit sphere

Recursive Bayesian tracking von Mises-Fisher filter
(4) Following via visual servoing
(5) Conclusion

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## Introduction

- working with a $360^{\circ}$ field-of-view


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- widely utilized sensor in navigation, SLAM, visual odometry


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- working with a $360^{\circ}$ field-of-view
- widely utilized sensor in navigation, SLAM, visual odometry
- additional cue in sensor fusion
- robust moving object detection and tracking


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## Omnidirectional image

- spherical projection model
[Geyer and Daniilidis, 2000, Barreto and Araújo, 2001]
- unifies image formation in central catadioptric systems and (in practice) fish-eye lenses [Ying and Hu, 2004]



## Spherical projection model



## Calibration

- method proposed in [Mei and Rives, 2007]
- from pixel to a point on the sphere

$$
\left.\begin{array}{rl}
\boldsymbol{m} & =\mathbf{K}^{-1} \boldsymbol{p} \\
\boldsymbol{P}_{n} & =\left[\begin{array}{l}
\frac{\xi+\sqrt{1+\left(1-\xi^{2}\right)\left(x^{2}+y^{2}\right)}}{x^{2}+y^{2}+1} x \\
\frac{\xi+\sqrt{1+\left(1-\xi^{2}\right)\left(x^{2}+y^{2}\right)}}{x^{2}+y^{2}+1} \\
\frac{\xi+\sqrt{1+\left(1-\xi^{2}\right)\left(x^{2}+y^{2}\right)}}{x^{2}+y^{2}+1}
\end{array}\right]
\end{array}\right] .
$$

## Moving object detection

- optical flow is a confluence of camera motion, independent object motion, and the 3D structure of the scene [Palmer, 1999]
- corner detection and pyramidal Lucas-Kanade algorithm (sparse optical flow) [Bouguet, 2000]
- discrimination based on odometry (no depth information)


## Camera displacement



## Flow vector clustering

- disjoint-set union find algorithm
- each cluster yields a point on the sphere




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## Recursive Bayesian tracking

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- prediction via

$$
p\left(\boldsymbol{x}_{k} \mid \boldsymbol{z}_{1: k-1}\right)=\int p\left(\boldsymbol{x}_{k} \mid \boldsymbol{x}_{k-1}\right) p\left(\boldsymbol{x}_{k-1} \mid \boldsymbol{z}_{1: k-1}\right) \mathrm{d} \boldsymbol{x}_{k-1}
$$

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$$

- correction via Bayes rule

$$
p\left(\boldsymbol{x}_{k} \mid \boldsymbol{z}_{1: k}\right)=\frac{p\left(\boldsymbol{z}_{k} \mid \boldsymbol{x}_{k}\right) p\left(\boldsymbol{x}_{k} \mid \boldsymbol{z}_{1: k-1}\right)}{p\left(\boldsymbol{z}_{k} \mid \boldsymbol{z}_{1: k-1}\right)}
$$

## von Mises-Fisher distribution

- a distribution on the unit sphere

$$
p(\boldsymbol{x} ; \kappa, \boldsymbol{\mu})=\frac{\kappa}{4 \pi \sinh \kappa} \exp \left(\kappa \boldsymbol{\mu}^{\mathrm{T}} \boldsymbol{x}\right),
$$

where $\boldsymbol{\mu}$ is the mean direction vector and $\kappa$ is the concentration parameter


## Tracking with the vMF [Chiuso and Picci, 1998]

- prediction-solve the integral

$$
\begin{aligned}
\boldsymbol{\mu}_{k \mid k-1} & =\boldsymbol{\mu}_{k-1} \\
\kappa_{k \mid k-1} & =A^{-1}\left(A\left(\kappa_{k-1}\right) A\left(\kappa_{Q}\right)\right), \quad A(\kappa)=\frac{1}{\tanh \kappa}-\frac{1}{\kappa}
\end{aligned}
$$

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$$

- correction-calculate the Bayes rule

$$
\begin{aligned}
\boldsymbol{\mu}_{k \mid k} & =\frac{\kappa_{k \mid k-1} \boldsymbol{\mu}_{k \mid k-1}+\kappa_{R} \boldsymbol{z}_{k}}{\kappa_{k \mid k}} \\
\kappa_{k \mid k} & =\sqrt{\kappa_{k \mid k-1}^{2}+\kappa_{R}^{2}+2 \kappa_{k \mid k-1} \kappa_{R}\left(\boldsymbol{\mu}_{k \mid k-1} \cdot \boldsymbol{z}_{k}\right)}
\end{aligned}
$$



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## Visual servoing [Chaumette and Hutchinson, 2008]

- cylindrical coordinates in the image [Iwatsuki and Okiyama, 2005, Fomena, 2008]

$$
\left[\begin{array}{l}
\dot{\rho} \\
\dot{\theta}
\end{array}\right]=\left[\begin{array}{cc}
\frac{-\cos \theta}{P_{z}} & 0 \\
\frac{-\sin \theta}{\rho P_{z}} & -1
\end{array}\right]\left[\begin{array}{c}
v \\
\omega
\end{array}\right]=\mathbf{L}_{s}\left[\begin{array}{c}
v \\
\omega
\end{array}\right]
$$

- control law

$$
\left[\begin{array}{c}
v \\
\omega
\end{array}\right]=-\lambda \hat{\mathbf{L}}_{s}^{-1}\left[\begin{array}{l}
\rho-\rho^{*} \\
\theta-\theta^{*}
\end{array}\right]
$$

## Following via visual servoing



## Experiments



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## Conclusion

- detection and tracking of moving objects in omnidirectional images
- spherical representation - von Mises-Fisher tracker
- following via visual servoing


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## Thank you for your attention!

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## Distance to great circle arc



## Distance to great circle arc

- great circle arc defined by ${ }^{c} \boldsymbol{P},{ }^{c} \boldsymbol{P}_{\infty}$
- find closest point to matched ${ }^{C} \boldsymbol{P}_{m}$ on the great circle

$$
\begin{aligned}
\boldsymbol{P}^{\prime} & ={ }^{c} \boldsymbol{P}_{m}-\left({ }^{c} \boldsymbol{P}_{m} \cdot n\right) n, \quad n={ }^{c} \boldsymbol{P}_{m} \times{ }^{c} \boldsymbol{P}_{\infty} \\
{ }^{c} \boldsymbol{Q}_{m} & =\frac{\boldsymbol{P}^{\prime}}{\left|\boldsymbol{P}^{\prime}\right|}
\end{aligned}
$$

- check if in the lune $\left({ }^{c} \boldsymbol{P},{ }^{c} \boldsymbol{P}_{\infty}\right)$

$$
\begin{aligned}
& \left({ }^{c} \boldsymbol{P} \times{ }^{c} \boldsymbol{Q}_{m}\right) \cdot\left({ }^{c} \boldsymbol{Q}_{m} \times{ }^{c} \boldsymbol{P}_{\infty}\right)>0 \& \& \\
& \left({ }^{c} \boldsymbol{P} \times{ }^{c} \boldsymbol{Q}_{m}\right) \cdot\left({ }^{C} \boldsymbol{P} \times{ }^{c} \boldsymbol{P}_{\infty}\right)>0
\end{aligned}
$$

- great circle distance

$$
d(\boldsymbol{P}, \boldsymbol{Q})=\arccos (\boldsymbol{P} \cdot \boldsymbol{Q})
$$

